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	Dominique Claveau-Mallet, Benoit Courcelles, Philippe Pasquier, & Yves Comeau
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Mention légale: Legal notice:	© 2017. This is the author's version of an article that appeared in Water Research (vol. 126) . The final published version is available at https://doi.org/10.1016/j.watres.2017.09.032 . This manuscript version is made available under the CC-BY-NC-ND 4.0 license https://creativecommons.org/licenses/by-nc-nd/4.0/

Numerical simulations with the P-Hydroslag model to predict phosphorus removal 1 by steel slag filters 2 By Dominique Claveau-Mallet*, Benoît Courcelles, Philippe Pasquier, and Yves Comeau 3 4 Department of Civil, Geological and Mining Engineering, Polytechnique Montreal, Montreal, Quebec, 5 Canada, H3C 3A7 6 * corresponding author: Dominique.claveau-mallet@polymtl.ca 7 ABSTRACT The first version of the P-Hydroslag model for numerical simulations of steel slag filters is presented. 8 9 This model main original feature is the implementation of slag exhaustion behavior, crystal growth and 10 crystal size effect on crystal solubility, and crystal accumulation effect on slag dissolution. The model 11 includes four mineral phases: calcite, monetite, homogeneous hydroxyapatite (constant size and 12 solubility) and heterogeneous hydroxyapatite (increasing size and decreasing solubility). In the proposed 13 model, slag behavior is represented by CaO dissolution kinetic rate and exhaustion equations; while slag 14 dissolution is limited by a diffusion rate through a crystal layer. An experimental test for measurement of exhaustion equations is provided. The model was calibrated and validated with an experimental 15 program made of three phases. Firstly, batch tests with 300g slag sample in synthetic solutions were 16 17 conducted for the determination of exhaustion equation. Secondly, a slag filter column test fed with 18 synthetic solution was run for 623 days, divided into 9 cells and sampled at the end of the experiment. 19 Finally, the column was dismantled, sampled and analyzed with XRD, TEM and SEM. Experimental 20 column curves for pH, oPO₄, Ca and inorganic carbon were well predicted by the model. Crystal sizes 21 measured by XRD and TEM validated the hypothesis for homogeneous precipitation while SEM 22 observations validated the thin crystal layer hypothesis. 23 **KEYWORDS** 24 slag, phosphorus, wastewater treatment modelling, PHREEQC, hydroxyapatite, calcite, precipitation 25 **ABBREVIATIONS**

26	Symbol	Description
27	General abbrev	<u>iations</u>
28	BOF	Basic oxygen furnace
29	CW	Constructed wetands
30	EAF	Electric arc furnace
31	HRT_{V}	Hydraulic retention time of voids
32	MONtoHAP	Transformation of MON into HAP
33	o-PO ₄	Ortho-phosphates
34	SEM	Scanning electron microscope
35	TEM	Transmission electron microscope
36	TIC	Total inorganic carbon
37	WW	Wastewater
38	XRD	X-Ray diffraction
39	Abbreviations f	or mineral phases
40	CAL	Calcite CaCO₃
41	НАР	Hydroxyapatite Ca₅OH(PO₄)₃
42	HAP_HO	Primary hydroxyapatite via homogeneous precipitation Ca₅OH(PO₄)₃
43	HAP_HE	Primary hydroxyapatite via heterogeneous precipitation Ca₅OH(PO₄)₃
44	HAP2	Secondary hydroxyapatite via monetite transformation Ca ₄ OH ₂ (PO ₄):
45	MON	Monetite CaHPO ₄
46	Symbol	Description Units (value)
47	<u>Constants</u>	
48	a_{HAP_0}	HAP crystal size in homogeneous precipitation [m]
49	B_1 and B_2	Regression coefficients in $k_{\it diss}$ exhaustion function
50	D^*	Dispersivity (transport model) [cm]
51	\mathcal{D}_n Exchange fac	tor between effective and immobile porosity (transport model) [s-1]
52	k_{CAL}	CAL precipitation constant [mol CAL/s m² slag]
53	k_{HAP}	HAP precipitation constant [mol HAP/s m ² slag]
54	k_{MON}	MON precipitation constant [mol MON/s m² slag]
55	$k_{MONtoHAP}$	MONtoHAP precipitation constant [M HAP2/(M MON s)
56	K_{spCAL}	Solubility product for CAL [M²]

57	K_{spHAP_bull}	Bulk solubility product for HAP	$[10^{-57} \text{ M}^9]$
58	K_{spHAP_HO}	Solubility product for HAP_HO	[M ⁹]
59	K_{spMON}	Solubility product for MON	$[M^2]$
60	L_{HAP}	L/D ratio for columnar HAP crystals	[-]
61	mv_{exp}	Slag mass to water volume ratio in a batch test	[g/mL]
62	MW_{HAP}	HAP Molecular weight	[502 g/mol]
63	n	Total porosity in the slag filter	[-]
64	n_e	Effective porosity in the slag filter	[-]
65	n_{im}	Immobile porosity in the slag filter	[-]
66	P_1, P_2, P_3 a	and P_4 Regression coefficients in pH_{sat} exhaustion function	
67	R	Ideal gas constant	[8.31 J mol ⁻¹ K ⁻¹]
68	S	Slag specific surface	$[m^2/m^3]$
69	se_{HAP_0}	initial HAP seeds concentration	[seeds/L]
70	SI_c	Critical saturation index between HAP_HE and HAP_HO	[-]
71	T	Temperature	[K]
72	γ	HAP mean free surface energy	[87 mJ/m ³]
73	$ ho_{barr}$	Crystal concentration in the crystal barrier	[g crystal/m³]
74	$ ho_{HAP}$	HAP crystal density [3 600	0.000 g/m^3]
75	$ ho_{slag}$	Slag grain density	[3.8 g/mL]
76	Rates, fund	ctions and variables	
77	a_{HAP}	Mean HAP crystal size	[m]
78	b_{im}	Moles of an element in immobile porosity (transport model)	[mol]
79	С	Total dissolved concentration for an element (transport model)	[mol/kgw]
80	C_e	C in effective porosity (transport model)	[mol/kgw]
81	C_{im}	C in immobile porosity (transport model)	[mol/kgw]
82	СаОІ _{ватн}	Leached CaO in a acid bath	[mol/g]
83	CaO _{KTEST}	Leached CaO in a batch test	[mol/g]
84	$CaOl_{TOT}$	Cumulative leached CaO in a batch test	[mol/g]
85	D_{barr}	Diffusion coefficient in the crystal barrier	$[m^2/s]$
86	d_{barr}	Thickness of the crystal barrier	[m]
87	k_{diss}	Slag dissolution constant [mol 0	CaO/m² slag]

88	K_{spHAP_HE}	Solubility product for HAP_HE	[M ⁹]
89	pH_{sat}	Saturation pH in the slag filter	[-]
90	q Concentratio	n in the solid phase for an element (transport model)	[mol/kgw]
91	r_{CAL}	CAL precipitation rate	[M CAL/s]
92	r_{diff}	CaO diffusion rate through crystal barrier	[M CaO/s]
93	r_{diss}	Slag dissolution rate	[M CaO/s]
94	r_{HAP_HE}	Primary heterogeneous HAP precipitation rate	[M HAP/s]
95	r_{HAP_HO}	Primary homogenous HAP precipitation rate	[M HAP/s]
96	r_{MON}	MON precipitation rate	[M MON/s]
97	$r_{MONtoHAP}$	Secondary HAP precipitation rate	[M HAP2/s]
98	S_{HAP}	HAP molar specific surface	[m²/mol]
99	se_{HAP}	HAP seeds concentration	[units/L]
100	SF_{diff}	Step function in diffusion rate	[-]
101	SF_{diss}	Step function in dissolution rate	[-]
102	SF_{HAP_HE}	Step function in HAP_HE rate	[-]
103	SF_{HAP_HO}	Step function in HAP_HO rate	[-]
104	SI_{HAP_HE}	Saturation index for HAP_HE	[-]
105	SI_{HAP_HO}	Saturation index for HAP_HO	[-]
106	t	Time (transport model)	[s]
107	v	Pore water flow velocity (transport model)	[m/s]
108	x	1D distance (transport model)	[m]
109	X_{CaO}	Total leached CaO in the slag filter	[M]
110			
111	1 Introduction		
112	Steel slag filters are a	n effective and passive technology for phosphorus remov	val from wastewater,
113	allowing typical muni	cipal effluent o-PO4 concentration below 0.5 mg P/L (Koi	v et al., 2016). Design tools
114	for slag filters are not	yet developed and full scale slag filters cannot be impler	mented without expensive
115	pilot tests. The main i	ssue related to steel slag filter operation relies on filter e	xhaustion and a relatively
116	rapid drop of remova	l efficiency (Chazarenc et al., 2008). A tool providing the	effect of influent

composition and operational conditions (type and size of slag, influent flowrate, filter geometry) on slag filter effluent o-PO₄ concentration and longevity would facilitate the design of these systems. This paper presents the P-Hydroslag model, a new model adapted for steel slag filter simulations considering influent composition and void hydraulic retention time (HRT_v) while being compatible with accepted physicochemical modeling frameworks (Lizarralde et al., 2015; Mbamba, Batstone et al., 2015; Mbamba, Tait et al., 2015).

this method does not consider void precipitation and long-term changes in the material properties, explaining why isotherms could not yet predict correctly full-scale behavior. The k-C* model traditionally used for constructed wetlands (Kadlec and Wallace, 2009) successfully predicted steel slag filter performance (Barca et al., 2013). This method may be suitable for design, but it cannot estimate the lifetime of the filter. A general correlation between material CaO content and P retention capacity based on several studies was proposed by Vohla et al. (2011), highlighting the importance of CaO dissolution in retention mechanisms. Such a design tool, however, does not consider important aspects as CaO availability, HRTv or influent composition, leading to a prediction uncertainty that is not acceptable for design purpose. Finally, a predictive model based on several material properties, HRTv and inlet P concentration was proposed (Penn et al., 2016). This model's strengths were to consider both Fe-Al and Ca based materials, propose an empiric relationship between material buffering capacity and P retention capacity, and predict P retention for both lab-scale and pilot-scale systems. This model, however, did not include direct measurement of kinetic rates, and would not be compatible with general physicochemical modeling frameworks in wastewater treatment.

Two previous modeling studies were published in the recent years. The first study (Claveau-Mallet et al., 2012) qualitatively described concepts forming the basis of the model, including slag dissolution, hydroxyapatite precipitation, crystal formation and accumulation in voids, and effect of velocity on

crystal accumulation. In the second study (Claveau-Mallet et al., 2014), concepts were translated into a prototype model including mathematical equations for precipitation and slag exhaustion, and a proposition of laboratory protocol for slag characterization was presented. Numerical simulations of a slag filter were performed on the base of this prototype model without experimental program for calibration. Results were realistic but overestimated the filter longevity. Predictions from the 2014 prototype model were compared to full-scale real data in a recent study (Koiv et al., 2016) in which longevity was overestimated.

In this paper, the first full version of the P-Hydroslag (standing for Phosphorus-hydroxyapatite-slag) model is presented. The P-Hydroslag model is similar to the 2014 prototype model, with additional features for diffusion barrier and crystal growth, a refined characterization of exhaustion equations, and a complete model equation matrix. The objectives were to calibrate the P-Hydroslag model with experimental data and evaluate the validity and realism of the model.

2 Material and Methods

2.1 Slag media

5-10 mm electric arc furnace steel slag produced by Arcelor Mittal and provided by Minéraux Harsco (Contrecoeur, Canada) was used (33% Fe₂O₃, 30% CaO, 16% SiO₂, 12% MgO. 6% Al₂O₃ and 3% other metallic oxides). Its density (3.8) and specific surface (0.308 m²/g) were determined according to the ASTM C127-04 standard (ASTM, 2004) and the Brunauer, Emmet and Teller method (Lowell et al., 2004). Slag from the same source was previously studied by the authors' research team for wastewater treatment applications (Claveau-Mallet et al., 2015; Claveau-Mallet et al., 2013; Koiv et al., 2016) or modeling studies (Claveau-Mallet et al., 2014; Claveau-Mallet et al., 2012).

2.2 Column test

A vertical filter column filled with slag was fed from its base with a synthetic wastewater in a saturated mode for a total duration of 623 days at approximatively 25°C. The column size was 159 cm in length and 10 cm in internal diameter. The synthetic wastewater solution consisted of K_2HPO_4 , KH_2PO_4 , $NaHCO_3$ and $CaCl_2$ in tap water. The influent mean composition was pH of 7.80 \pm 0.2, ortho-phosphates (o-PO₄) of 8.9 \pm 2.0 mg P/L, total inorganic carbon (TIC) of 22 \pm 2 mg C/L, Ca of 54 \pm 14 mg/L and alkalinity of 102 \pm 3 mg $CaCO_3$ /L. The influent flowrate was 6.9 \pm 1.0 mL/min for the first 517 days and 3.4 \pm 0.5 mL/min for the remaining 106 days of operation.

The column was divided into 11 virtual cells for the filling step, identified #0 to #10, with #0 at bottom (inlet) and #10 at top (outlet). Cells #1 to #9 were 15 cm long and had a sampling hole in the middle.

Cells #0 and #10 were 7.5 cm long and had no sampling hole to provide a slag transition zone between the inlet/outlet tubing and sampling zones. While filling the column, two 300 g slag samples were taken from each cell using a standard sampling procedure for aggregate materials (ASTM C702, 2011). Slag samples were used in batch kinetic tests (presented in section 2.3). The total slag mass in the column was 24.24 kg, resulting in a 49.2% porosity.

The feeding barrel, column effluent and cells were sampled and analyzed periodically for pH, o-PO₄, filtered Ca, settled TIC, total P and alkalinity, using standard procedures (APHA, AWWA and WEF, 2005). A maximum of 3 cells were sampled in the same day to minimize perturbation, resulting in a monthly sampling frequency for each cell (twice a month in the second feeding phase). The feeding barrel and effluent column sampling frequency was weekly for pH and once or twice a month for the other parameters. Tracer tests were conducted after 12, 69, 82, 107, 187, 271, 376 and 558 days. Rhodamine at a concentration of 20 mg/L was used as a tracer and measured in the effluent using spectrofluorometry.

At the end of operation, feeding was stopped and the column was kept saturated for 6 days before dismantling. Upon dismantling, pore water was first sampled and analyzed, then the column was cut

into 4 sections to ensure efficient solids sampling. For each cell, three samples were taken: first, several slag particles sampled before doing any major disturbance of the slag media (for scanning electron microscope (SEM) analysis); then slag was washed with water in a large pan and precipitates were sampled by sedimentation (for X-ray diffraction (XRD) and transmission electron microscope (TEM) analyses); finally, a 300 g of washed slag sample was taken for kinetic tests (described in section 2.3). Precipitates were air-dried for 3 days, sieved at mesh 60 and cleaned from slag dust with a strong magnet. Precipitates were analyzed with XRD using a Philipps X'Pert diffractometer operated at 50 kV and 40 mA, using the Bragg-Brentano geometry and a Cuk_α radiation. The Scherrer equation (Cullity, 2001) was used to estimate mean crystal sizes from diffractograms, using the ~26.1° peak for hydroxyapatite (HAP) and ~29.4° peak for calcite (CAL). Precipitates of cells 1, 2, 3 and 8 were analyzed using TEM with the bright field imaging technique (Jeol JEM-2100f field emission gun microscope, 200 kV). Before TEM analysis, samples were prepared with a 30-s ultrasound bath in methanol, and placed on a copper grid covered with Formwar lightly coated with amorphous carbon. Undisturbed slag particles of cells 1, 2, 3, 5 and 8 were analyzed with SEM using a Jeol JSM-7600F microscope (2.0 kV, LEI or SEI detector).

2.3 Batch kinetic tests

The batch kinetic test method is described in another reference (Claveau-Mallet et al., 2014) and is intended to produce exhaustion equations. The batch test included 5 identical phases. In a phase, the slag sample was placed in a 1L Erlenmeyer flask containing 350 or 700 mL of a wastewater solution. The Erlenmeyer flask was placed in a gyratory shaker at 160 rpm. The flask was closed with a rubber cap that contained three airtight holes; one for a pH probe, one for a sampling tubing and one for a tubing connected to a N₂ gas balloon. The synthetic solution was composed of KH₂PO₄, K₂HPO₄, NaHCO₃ and CaCl₂ dissolved in tap or distilled water. Four solutions with different concentrations were used to test the method in a realistic range of wastewater types (pH of 6.5 to 7.9, o-PO₄ of 8 to 24 m P/L, Ca of 17 to

50 mg/L, TIC of 0.5 to 24 mg C/L and alkalinity of 3 to 107 mg CaCO₃/L). At time zero, slag was inserted. pH was monitored for 3 to 4 days. Three intermediary 20-mL samples were taken and analyzed for o-PO₄, filtered Ca and filtered TIC. When necessary, a linear correction against time was applied to pH measurements to account for probe drift. After this test, the slag sample was rinsed and immediately transferred to a 160 rpm shaken HNO₃ acid bath of known volume and concentration for 3 to 5 days. After the acid bath, pH was measured and the corresponding leached CaO from the slag was computed using numerical simulations (explained in section 2.5.2). After the acid bath, the slag sample was carefully rinsed and used again for a subsequent phase.

Each 300-g slag sample from cells 1 to 8 was used for a 5-phase kinetic test, resulting in 16 kinetic tests (2 replicates per cell). One-phase batch tests on dismantled column slag samples were performed for cells 1 to 9.

- 222 2.4 Model description
- 223 2.4.1 Precipitation

The model's Gujer matrix is presented in appendix. Three mineral phases are included: HAP typically found in slag filters (Baker et al., 1998), monetite (MON) as intermediary phase and CAL. The transformation of MON into HAP (MONtoHAP) was modelled as precipitation of HAP2, an artificial phase composed of ions missing from MON before being HAP. Precipitation rates for HAP, MON and CAL were formulated with a basic expression rate = $k \times SI$, with $k = k \times SI$, was set at $k \times SI$, was set at $k \times SI$, which $k \times SI$ is a constant normalized with slag surface and $k \times SI$. When $k \times SI$ is a constant normalized with slag surface and $k \times$

233 Appelo, 1999)) and hydrated calcium carbonate (10^{-7.144}, MINTEQ database (Allison et al., 1991)).

 K_{SpMON} was set at 10⁻⁷ from Valsami-Jones (Valsami-Jones, 2001).

Two types of HAP were included to account for two types of precipitation. HAP_HO was HAP formed by homogeneous precipitation (new seeds precipitated in voids, or spontaneous precipitation) while HAP_HE was HAP formed by heterogeneous precipitation (on existing surfaces - crystal growth). HAP_HE occurred below a critical saturation index (SI_c) while HAP_HO occurred over SI_c . In homogeneous precipitation, crystal size was assumed to be constant. Using equation 1 for solubility of fine particles (Stumm and Morgan, 1996b), K_{sphAP_HO} was set at 10^{-46} . Temperature was set at 298 K and specific surface (S_{HAP}) was calculated assuming crystal size $a_{HAP_0} = 31.3$ nm, columnar shape for HAP and a L/D ratio (L_{HAP}) of 50. The value assumed for a_{HAP_0} is close to crystal size measured in this study (presented in a following section) and measurements made in previous studies (Claveau-Mallet et al., 2012, 2013). A value of 10^{-46} for K_{sphAP_HO} is consistent with equilibrium state generally observed in slag filters, assumed when effluent pH is over 10 with high HRT $_V$ (Table 1 and Figure 1). In Table 1, Ca^{2+} , OH^- and PO_4^{3-} activities were determined with PHREEQC and used for apparent solubility calculation. Studies conducted with hydrated oil shale ash were included in Table 1 as they behave in a similar way then slag. Resulting mean and median were $10^{-45,7}$ and $10^{-46,0}$ from 389 data points.

$$249 \qquad log(K_{spHAP_{HO}}) = log(K_{spHAP_{bulk}}) + \frac{\frac{2}{3}\gamma S_{HAP}}{2.3RT}$$
[1]

Table 1. Apparent HAP solubility from reported alkaline filter effluent with pH≥10, based on reported
 pH, Ca and o-PO₄ concentration.

Material	Size	Influent	Type of study HAP	Nb of data			
iviateriai	(mm)	imiuent		mean	median	f	point s
			lab –				
Sas	5-10	Solution	column	-45.55	-45.94	1	35

			lab –				
EAF slag	5-10	Solution	column	-45.18	-45.72	2	103
			lab –				
Sas	2.5-5	Solution	column	-48.06	-48.17	3	6
			pilot –				
Sas	5-10	real fishfarm WW	column	-45.23	-45.39	4	46
Hydr. Oil shale ash	5-20	real domestic WW	pilot – CW	-46.32	-46.52	5	62
		real landfill					
Hydr. Oil shale ash	5-20	leachate	pilot – CW	-46.55	-46.42	5	97
		reconst. fishfarm					
ladle furnace slag	0-1	WW	lab – CW	-44.86	-45.28	6	9
Sas mixed with		reconst. fishfarm					
limestone	5-15	WW	lab – CW	-46.04	-46.01	6	12
Sas mixed with		reconst. fishfarm					
limestone	20-40	WW	lab – CW	-44.48	-44.56	6	8
		reconst. domestic					
Sas	10-30	WW	lab – CW	-40.85	-41.01	7	11
		reconst. domestic					
Sas	30-100	WW	lab – CW	-45.16	-45.26	7	8*
	0.003-		lab –				
BOF oxide mixture	0.1	Solution	column	-49.51	-49.47	8	8*
EAF slag	20-40	real domestic WW	pilot – CW	-44.07	-	9	* +
BOF slag	20-40	real domestic WW	pilot – CW	-43.52	-	9	* +

^{*:} all data below pH 10 for these studies. Data was not considered for calculation of global K_{sp}

Sas: same as present study; WW: wastewater; CW: constructed wetland

Ref #1: Claveau-Mallet et al., 2012. Ref #2: Claveau-Mallet et al., 2013. Ref #3: Forget, 2001. Ref #4:

Koiv et al., 2016. Ref #5 : Koiv et al., 2010. Ref #6 : Abderraja Anjab, 2009. Ref #7 : Stangart, 2012. Ref

#8: Baker et al., 1998. Ref #9: Barca et al., 2013.

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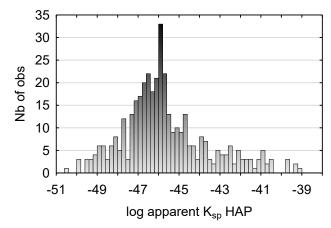


Figure 1. Apparent HAP solubility distribution for all reported studies (pH \geq 10; 389 observations).

^{+:} single K_{sp} calculated from reported mean values for pH, o-PO₄ and Ca

In heterogeneous precipitation, crystal size is a variable following crystal growth on existing seeds, assuming that all crystals have the same size. The number of seeds (se_{HAP}) increases as homogeneous precipitation takes place, assuming an initial number of seeds (se_{HAP}) and columnar shape. Equations for HAP_HE specific surface and solubility product are provided in equations 2 and 3.

$$264 \quad log(K_{spHAP_HE}) = log(K_{spHAP_bulk}) + \frac{\frac{2}{3}\gamma S_{HAP}}{2.3RT}$$
 [2]

265
$$S_{HAP} = \frac{(4L_{HAP} + 2)MW_{HAP}}{a_{HAP}\rho_{HAP}}$$
 [3]

266 2.4.2 Slag dissolution

Slag composition was simplified to the chemical formula CaO-0.3CaCl $_2$. Exhaustion equations were determined experimentally (described later), resulting in decreasing functions for saturation pH (pH_{sat}) and dissolution kinetic constant (k_{diss}). k_{diss} was normalized with slag surface as for precipitation constants. The proposed approach gives flexibility to the model and every specific slag has its own exhaustion parameters determined from batch tests by regression.

Schwartz, 1998) through a crystal barrier that forms uniformly on the slag surface in a thin layer. The thickness of the crystal barrier (d_{barr}) increased according to CAL, HAP and MON precipitation, assuming a constant specific surface (S) for slag (equation 4). It was assumed that the type of precipitation has an influence on the diffusion coefficient (D_{barr}) and that diffusion is easier in a large and organized crystals framework, compared to numerous small crystals. Mathematically, D_{barr} was defined with a step function set initially at a high value, and to a lower value when the seed concentration was doubled. As either dissolution or diffusion rate is the limiting process (the smallest), the step function was added to consider the passage from dissolution-limiting to diffusion-limiting.

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$$d_{barr} = \frac{(m_{CAL} + m_{HAP} + m_{MON}) \times n}{\rho_{barr} S \times 0.001(1-n)}$$
 [4]

282 2.4.3 Hydraulic model

In continuous flow column simulations, the Advection-Reaction-Dispersion (ARD) equation for 1D flow
was used (equation 5). A first-order exchange approximation was added to account for diffusion
between effective and immobile porosity (equation 6). The hydraulic model is available in the PHREEQC
software (Parkhurst and Appelo, 1999).

$$287 \qquad \frac{\partial C}{\partial t} = -v \frac{\partial C}{\partial x} + D^* v \frac{\partial^2 C}{\partial x^2} - \frac{\partial q}{\partial t}$$
 [5]

$$288 \qquad \frac{db_{im}}{dt} = n_{im} \left(1 + \frac{dq}{dC} \right) \frac{dC_{im}}{dt} = D_n (C_e - C_{im})$$
 [6]

- 289 2.5 Numerical simulations
- Numerical simulations were performed using the PHREEQC software with its IPHREEQC modules for interfacing with MATLAB (Charlton and Parkhurst, 2011).
- 292 2.5.1 Batch tests

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The initial solution was simulated with KH₂PO₄, K₂HPO₄, CaCl₂ and NaHCO₃ added to pure water. A small 293 294 amount of HCl or NaOH was included to reproduce the precise pH of the experimental solution. 295 Solutions were equilibrated with HAP and CAL (but no MON) in the EQUILIBRIUM PHASES block prior to 296 the simulated batch test. Simulated and experimental alkalinity were used for calibration of initial 297 solutions. Slag exhaustion was considered to be constant, therefore, pH_{sat} and k_{diss} were constant 298 instead of being adjusted according to exhaustion equations. pH_{sat} was set as the maximum pH value 299 reached in the experimental batch test. Calcite precipitation was removed from the batch test model, as 300 surprisingly no calcite precipitation occurred in experimental batch tests (no TIC reduction).

The model constants were identified by minimizing the misfit between the simulated output and the experimental pH and oPO_4 measurements. The objective function optimization was performed on the log transformed constants k_{diss} , k_{HAP} , k_{MON} , $k_{MONtoHAP}$ and CaO_{in} with the conjugate gradient

method and the golden-section search method (Press, 2007). As shown in Table 2, a two-step strategy was used to achieve satisfactory results and speed-up the calibration process. In the first step, the mean absolute error between the experimental and simulated pH (F_1) was minimized with large tolerances for PHREEQC (1E-11) and the optimization algorithm (1E-7 for line search and 0.01 as F stop criteria). Then, the objective function F_2 was minimized with more demanding tolerances (1E-12 for PHREEQC and line search, and 0.001 as F stop criteria). Note that CaO_{in} was a little amount of CaO instantaneously released at the water/slag contact, added for improving the calibration.

Table 2. Batch test inversion parameters for conjugate gradient method

Step	Initial values (log)	Objective function
1	-7 for k_{diss} and CaO_{in} -6.5 for k_{MON} -9 for k_{HAP} and $k_{MONtoHAP}$	$F_{1} = \frac{1}{n} \sum_{i=1}^{n} pH_{i,exp} - pH_{i,sim} $
2	Solution from inversion 1	$F_{2} = F_{1} + \frac{0.2}{m} \sum_{1}^{m} \left oPO_{4_{m,exp}} - oPO_{4_{m,sim}} \right $

2.5.2 Exhaustion functions

Exhaustion functions were produced by plotting pH_{sat} and k_{diss} against total leached CaO ($CaOl_{TOT}$). For a given phase i, $CaOl_{TOT}^i$ was calculated by cumulating leached CaO in preceding kinetic tests and acid bath (equation 7). $CaOl_{BATH}$ was determined by simulating acid bath with PHREEQC, following the final pH of the acid bath as a target value.

318
$$CaOl_{TOT}^{i} = 0.5 \times CaO_{KTEST}^{i} + \sum_{n=1}^{i-1} (CaO_{KTEST}^{n} + CaO_{BATH}^{n})$$
 [7]

Exhaustion functions coefficients were determined by linear regression of pH_{sat} vs $CaOl_{TOT}$ (equation 8) and logistic function regression of k_{diss} vs $CaOl_{TOT}$ (equation 9). Mean regression coefficients were kept for k_{diss} , but coefficients following the top of the graphical data cloud were kept for pH_{sat} , as

 pH_{sat} is a saturation state, and we can assume that saturation is controlled by the most reactive

323 particles.

324
$$pH_{sat} = P_2 - \frac{P_2 - P_1}{\left(1 + e^{-P_3(CaOl_{TOT} - P_4)}\right)}$$
 [8]

$$325 k_{diss} = B_1 + B_2 CaOl_{TOT} [9]$$

- 326 In the Gujer matrix, exhaustion functions included additional terms involving porosity and slag density to
- account for the conversion of $CaOl_{TOT}$ (units of mol/g slag) into X_{CaO} (units of mol/L water) for filter
- 328 numerical simulations.
- 329 2.5.3 Column test
- 330 The simulated influent was prepared according to the procedure described in the batch tests section.
- 331 The column test was simulated within KINETIC and TRANSPORT blocks, with 50 numerical cells and a
- tolerance of 1E-6. Kinetic rates were applied to both mobile and immobile cells. Hydraulic parameters
- 333 n_e , D^* and D_n were calibrated with each tracer test.
- 334 3 Results and discussion
- 3.1 Determination of exhaustion equations and precipitation constants
- In general, batch test calibration was excellent for pH and good for o-PO₄, except for the period 0 to 100
- min where the model overestimated slightly the o-PO₄ concentration. An example of a well-calibrated
- batch test (rank 7 out of 84 for global error function) is shown in Figure 2. No TIC reduction was
- observed. Absence of CAL precipitation in batch tests was not expected, as calcite was precipitated in
- column tests and is frequently observed in slag filters (Claveau-Mallet et al., 2013; Liira et al., 2009).
- Mean precipitation constants were $k_{HAP} = 10^{-11.03} \, mol \, HAP/s \, m^2 slag$, $k_{MON} =$
- $10^{-8.67} \, mol \, MON/s \, m^2 slag \, and \, k_{MONtoHAP} = 10^{-8.01} \, mol \, HAP2/s \, mol \, MON.$

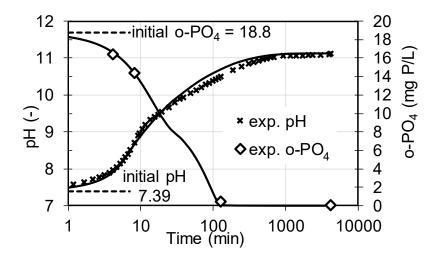


Figure 2. Example of a batch test calibration. Simulated data is shown with lines. Batch test error functions: 0.09 for pH and 0.15 for o-PO₄.

pH_{sat} and k_{diss} obtained from all batch tests were plotted against CaOl_{tot} for the production of exhaustion functions (Figure 3). For k_{diss} , linear regression coefficients were used in column simulations (B₁ = -7.91 and B₂ = -1933 g/mol). pH_{sat} exhaustion function had to be slightly increased above the data cloud (discussed later) to improve the calibration (Figure 3B), resulting in coefficients P₁ = 9.1, P₂ = 12.1, P₃ = 6000 and P₄ = 1.2E-4.

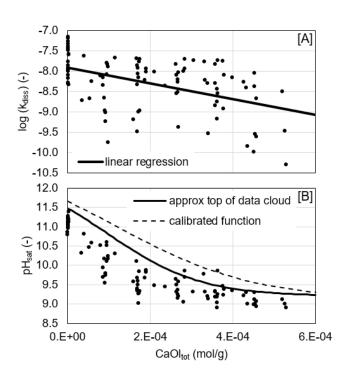


Figure 3. Exhaustion functions for k_{diss} (A) and pH_{sat} (B). Regression coefficients are provided in text.

3.2 Column test calibration

An example of tracer test calibration is shown in appendix. Hydraulic parameters D^* (dispersivity) and D_n (exchange factor between mobile and immobile porosity) were roughly constant for 8 tracer tests, while effective porosity (n_e) decreased slightly following the column operation. The n_e decrease was neglected, and hydraulic parameters from tracer test at time 187 were used $(n_e=0.359, D^*=5 \text{ cm} \text{ and } D_n=5 \text{x} 10^{-6} \text{ s}^{-1})$.

Results of numerical simulations are compared to experimental data in Figure 4. pH was correctly predicted for cells 1 to 6 but slightly underestimated for cells 7 to effluent. o-PO₄ was in general successfully predicted, except for cells 1 and 2 in the first 100-200 days, where the o-PO₄ rise was predicted too late. This could be explained by the close position of cells 1 and 2 relative to the influent point resulting in a non plug flow condition for these cells and in some short-circuiting. Calibration of o-PO₄ from cells 5 to 7 was less accurate for the last 100 days, as the model predicted a stable concentration while the experiment showed an increase of almost an order of magnitude. Calcium and TIC calibration were less accurate then those for pH and o-PO₄, but were considered satisfactory. The effect of the influent rate change was correctly predicted by the model.

Calibrated constants were $k_{CAL}=10^{-9}\frac{M}{s\,m^2}$, $SI_c=0.2$ and $\rho_{barr}=2000\frac{kg}{m^3}$. Precipitation constants for HAP, MON and MONtoHAP were already determined in batch tests and were not changed for column simulations. SI_c was lower than reported values for calcite, which occurs in heterogeneous precipitation over $SI_c=0.3$ and homogeneous precipitation over $SI_c=1.5$ (Mayes et al., 2006). ρ_{barr} value was similar to dry density for a natural sand. k_{CAL} was 2.5 orders of magnitude higher than the reported initial value by Mbamba, Tait et al (2015), and monetite constant was in the same order of magnitude as Mbamba's values. In this study, precipitation rates were function of crystal concentration,

with initial crystal seeds of 1E-5 M, while the effect of crystal concentration was not considered in this model.

The column was divided in two zones for the calibration of se_{HAP_0} : cells 1 to 6 were set at 2e21 seeds/L and cells 7 to 9 (and all immobile cells) were set at 5e20 seeds/L. This refinement was necessary to achieve both o-PO₄ calibration of first cells (mainly homogeneous precipitation) and last cells (mainly heterogeneous precipitation). Attributing different se_{HAP_0} values for two zones was considered realistic because it represents a crystal behavior in which at a very low supersaturation index, fewer but bigger crystals are formed. This behavior was confirmed during column dismantling. In cells 8 and 9, a very small amount of precipitates was observed and sampled, with fresh- and unused-looking slag. Several well-formed crystals could be seen by naked eyes only in cells 8 and 9 (3-4 mm in length).

The implementation of the diffusion equation is considered a major improvement compared to previous prototype versions of the model. Without the diffusion equation, CaO would always be leached at its maximum capacity (pH_{sat}) and longevity would be highly overestimated. D_{barr} calibration was 1E-10 m²/s at first and was decreased to 5E-16 m²/s when the seed concentration was doubled. Calibrated values of D_{barr} for the two steps are similar to diffusion coefficients observed for clays. A large range was reported for radioactive waste storage applications: from 10^{-17} to > 10^{-13} m²/s in consolidated clay

(Alonso et al., 2009) and 10^{-11} to 10^{-10} m²/s in altered bentonite (Manjanna et al., 2009).

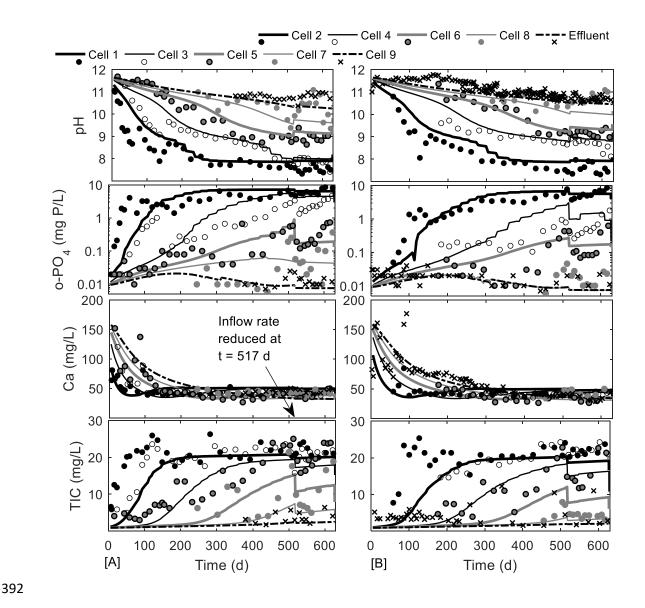


Figure 4. Water composition in a column test for cells 1 to 9 (A) and cells 2 to effluent (B). Experimental data is shown with dots or x and simulated data with lines.

3.3 Validation of model hypothesis

The diffusion equation can be validated by the robustness of the model regarding pH. The model could predict pH at the end of operation, pH after the 6-day rest and pH_{sat} (Figure 5). pH was slightly underestimated for pH_{sat} and pH after rest, but relative trends for pH and pH_{sat} were properly predicted, as well as the pH increase induced by the 6-day rest. The crystal layer was realistic as uniform crystal

deposits were observed by SEM (Figure 6). The presence of cracks induced by air-drying was also suggesting that a crystal suspension layer was present onto the slag surface. Uniformity of crystal composition was confirmed by TEM-EDS as CAL and HAP were frequently found in the same crystal at nanometric scale.

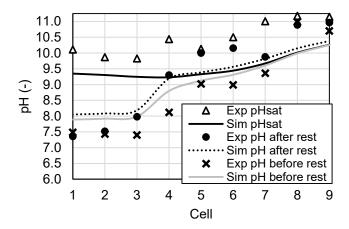


Figure 5. pH distribution within column at the end of operation (623 days of feeding followed by 6 days of rest).

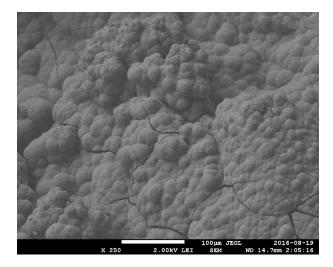


Figure 6. SEM picture of slag grain surface from cell 2 at dismantling.

Cristal size in homogeneous precipitation was confirmed by microscope observations. In cells 1 to 3, where the amount of precipitated HAP was sufficient for measurements, isolated crystals in TEM

pictures were measured, resulting in a 35 nm mean value for 505 measurements. A similar value of 24 nm was calculated from XRD diffractograms of cells 1 to 3. No specific increase was observed in crystal size from cells 1 to 3, validating the constant crystal size hypothesis for homogeneous precipitation. HAP composition was confirmed by XRD patterns (provided in supporting information). HAP composition for individual crystals from TEM was confirmed by P and Ca presence with EDS. No monetite was detected by XRD and no monetite precipitation occurred in the column simulations while monetite was precipitated in batch test simulations, suggesting that pH rise in column was too fast for monetite formation.

The relative small amount of formed HAP in heterogeneous precipitation made impossible XRD or TEM crystal size analysis for heterogeneous HAP. It was possible, however, to analyse the progression of calcite crystal size within the column using XRD. Its size was around 200 nm in cells 1 to 3, increased to 900 nm in cell 5, and was over the limit of Scherrer equation in cells 6 and higher. This suggests homogeneous precipitation and constant size in the first cells and heterogeneous precipitation and crystal growth in last cells.

Even if a distinction between homogeneous and heterogeneous precipitation was made for calcite, its solubility was kept constant for both conditions. Assuming homogeneous precipitation at 200 nm (as measured in cells 1 to 3) and spherical crystals, the computed solubility product from equation 1 is very close to bulk solubility. While HAP growth decreases its solubility, CAL homogeneous crystals are large enough to neglect this effect.

3.4 Model limits and recommendations

The main issue regarding the model is the number of batch kinetic tests needed to provide exhaustion equations. The hypothesis of most reactive grains in batch tests conditioning column tests should also be examined, because even if pH_{sat} exhaustion equation was overestimating experimental data, pH in

the last cells of columns were underestimated. Work should be done using statistical analysis and theory of artificial granular material sampling (Gy, 1979) for reducing the number of batch tests and transposing correctly batch to column conditions.

Calibration of heterogeneous precipitation was limited by experimental data, as last cells did not reach their longevity. Additional studies involving long-term operation of slag filters and breakthrough of last sections of filters, in which heterogeneous precipitation occurred for a while, would be needed for accurate calibration and in-depth study of seeds concentration and type of precipitation. In this paper, two layers of different seeds concentration were proposed, but other formulations would be possible including step functions for seeds VS saturation index, increasing the number of layers or adding a third type of HAP.

Further work should be conducted regarding need for refinement of the model. Additional features such as interaction with atmospheric CO_2 or porosity reduction (Courcelles et al., 2011) may be needed in some cases as constructed wetlands. The model could be improved with additional P species (Mbamba, Tait, et al., 2015) or consideration of crystal surface in rate equations. Crystal surface is obviously increasing in this type of process, with long operation time without extraction, but kinetic parameters may be less important than saturation parameters (pH_{sat} and K_{spHAP_HE}). Sensitivity analyses would be needed to assess which aspect should be studied further, slag dissolution kinetics, crystal equilibrium parameters or crystal kinetic parameters.

4 Conclusion

The first version of the P-Hydroslag model that can be used for prediction of steel slag filter efficiency and longevity was presented in this paper. The objectives were to calibrate the model with experimental data and evaluate the validity and realism of the model. The main outcomes were as follows:

- A complete model equation matrix was provided. The model included two main kinetic equation sets: a first set for CaO dissolution and a second set for precipitation. CaO dissolution equations included slag exhaustion and CaO diffusion through a uniform crystal barrier on slag particles. Precipitation equations included calcite precipitation, monetite precipitation, transformation of monetite into hydroxyapatite, homogeneous hydroxyapatite precipitation (constant size) and heterogeneous hydroxyapatite precipitation (increasing size). An equation for hydroxyapatite solubility related to crystal size was included. Standard equilibrium reactions were included in the model via the PHREEQC software. The advection-diffusion-reaction model was used as the hydraulic model (1D porous media transport).
- The crystal barrier hypothesis was confirmed by SEM observations of used slag grains.

 Homogeneous and heterogeneous precipitation hypothesis was confirmed by TEM crystal size count and XRD measurements.
- The model and proposed experimental procedure for characterization of slag exhaustion behavior were successful in producing realistic results. Numerical simulations reproduced experimental breakthrough curves (pH, o-PO₄, Ca, TIC) of an upward flow column slag filter.

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Appendix

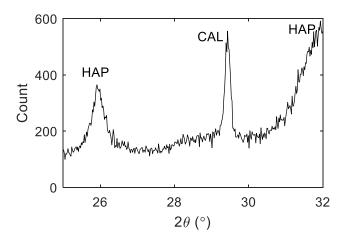


Figure A1. XRD pattern of precipitates sampled in cell #2. Main peaks of HAP and CAL diffractograms are indicated in the figure

 Table A1. P-Hydroslag model matrix

Phase	Stoichiometry -		etry - aq	ueous		Stoichiometry – mineral phases				Rate equation	Equilibrium constants	
	H ⁺	OH-	Ca ²⁺	CO3 ²⁻	PO ₄ ³⁻	Cl-	HAP	MON	CAL	HAP2		
											$r_{HAP_HO} = 0.001k_{HAP}S\frac{(1-n)}{n} \times SI_{HAP_HO} \times SF_{HAP_HO}$	
Primary homogenous hydroxyapatite (HAP HO)		-1	-5		-3		+1				$SI_{HAP_HO} = log\left(\frac{\{Ca^{2+}\}^5\{PO_4^{3-}\}^3\{OH^-\}}{K_{spHAP_HO}}\right)$	$pK_{spHAP_HO} = 46$
(1111 _110)											$SF_{HAP_HO} = \frac{1}{1 + e^{-50\left(log(SI_{HAP_HO}) - log(SI_c)\right)}}$	
											$r_{HAP_HE} = 0.001k_{HAP}S\frac{(1-n)}{n} \times SI_{HAP_HE} \times SF_{HAP_HE}$	
Primary heterogeneous hydroxyapatite (HAP HE)		-1	-5		-3		+1				$SI_{HAP_HE} = log\left(\frac{\{Ca^{2+}\}^5\{PO_4^{3-}\}^3\{OH^-\}\}}{K_{SpHAP_HE}}\right)$	$log(K_{spHAP_HE})$ $= log(K_{spHAP_bu})$ $+ \frac{2}{3} \gamma S_{HAP}$ $+ \frac{2}{3} \gamma S_{HAP}$
(11111_112)											$SF_{HAP_HE} = 1 - \frac{1}{1 + e^{-50(log(SI_{HAP_HO}) - log(SI_c))}}$	2.3 <i>RT</i>
Monetite (MON)	-1		-1		-1			+1			$r_{MON} = 0.001 k_{MON} S \frac{(1-n)}{n} \times log \left(\frac{\{Ca^{2+}\}\{HPO_4^{2-}\}\}}{K_{spMON}} \right)$	$pK_{spMON} = 7$
Calcite (CAL)			-1	-1					+1		$r_{CAL} = 0.001 k_{CAL} S \frac{(1-n)}{n} \times log \left(\frac{\{Ca^{2+}\}\{CO_3^{2-}\}\}}{K_{SpCAL}} \right)$	$pK_{spCAL} = 6.8$
Secondary hydroxyapatite* (HAP2)		-2	-4		-2					+1	$r_{MONtoHAP} = k_{MONtoHAP} \times SI_{HAP_HO}[MON]$	$pK_{spHAP_HO} = 46$

^{*:} transformation of monetite into hydroxyapatite

Table A1 (followed). Complete P-Hydroslag model matrix

Slag dissolution	+2	+1.3		+0.			$r_{diss} = A \times SF_{diss}$	N/A
				3			$A = 0.001k_{diss}S\frac{(1-n)}{n}\left(\frac{pH_{sat} - pH}{pH_{sat}}\right)$	
							$SF_{diss} = 1 - \frac{1}{1 + e^{-50(A - B)}}$	
							$r_{diff} = B \times SF_{diff}$	
CaO diffusion							$B = \frac{0.5 \times D_{barr} \times (10^{pH_{Sat}-14} - \{OH^{-}\})}{d_{barr}} \times \frac{S \times 0.001(1-n)}{n}$	
through crystal barrier	+2	+1					$SF_{diff} = \frac{1}{1 + e^{-50(A-B)}}$	N/A
							$log(D_{barr}) = -10 - 5.3 \times \frac{1}{1 + e^{-50\left(\frac{Se_{HAP}}{Se_{HAP}_{-0}} - 2\right)}}$	

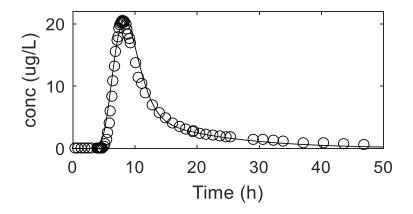


Figure A2. Tracer test experimental data (circles) and numerical calibration (line) (started at Time = 187 d of filter operation)

Detailed equations to complement the model matrix

- 2 Advection-reaction-dispersion (ARD) equation for 1D transport and First-order exchange
- 3 approximation between effective and immobile porosity:

$$4 \qquad \frac{\partial c}{\partial t} = -v \frac{\partial c}{\partial x} + D^* v \frac{\partial^2 c}{\partial x^2} - \frac{\partial q}{\partial t}$$
 [A1]

$$5 \qquad \frac{db_{im}}{dt} = n_{im} \left(1 + \frac{dq}{dC} \right) \frac{dC_{im}}{dt} = D_n (C_e - C_{im}) \tag{A2}$$

6 Detailed equations for HAP_HE:

$$S_{HAP} = \frac{(4L_{HAP} + 2)MW_{HAP}}{a_{HAP}\rho_{HAP}}$$
 [A3]

8
$$a_{HAP} = \frac{[HAP_HE]MW_{HAP}L_{HAP}^2}{\rho_{HAP}^3\sqrt{se_{HAP}}} + \sqrt[3]{se_{HAP}^2}a_{HAP_0}^3$$
 [A4]

9
$$se_{HAP} = se_{HAP_0} + \frac{[HAP_0]MW_{HAP}L_{HAP}^2}{\rho_{HAP}\alpha_{HAP_0}^3}$$
 [A5]

10 Detailed equations for diffusion through crystal barrier:

$$11 \qquad d_{barr} = \frac{(100[CAL] + 502[HAP] + 136[MON] + 366[HAP2]) \times n}{\rho_{barr} S(n-1)} \tag{A6} \label{eq:A6}$$

12 Detailed equations for exhaustion functions:

13
$$pH_{sat} = P_2 - \frac{P_2 - P_1}{\left(1 + e^{-\frac{P_3}{F}(CaOl_{TOT} - F \times P_4)}\right)}$$
 [A7]

14
$$log(k_{diss}) = B_1 + \frac{1}{F}B_2X_{CaO} + log\left(0.001S\frac{(1-n)}{n}\right)$$
 [A8]

15
$$F = \frac{1000\rho_{slag}(1-n)}{n}$$
 [A9]